Answer each of the following showing all work.

1. Find the area of the region bounded by the graphs of $y=x^{2}+2, y=-x, x=0$, and $x=1$.
2. Find the area of the region between the graphs of $f(x)=3 x^{3}-x^{2}-10 x$ and $g(x)=-x^{2}+2 x$.
3. Find the volume of the solid generated by revolving about the $x$-axis the region bounded by $y=x^{2}$ and $y=2-x^{2}$.
4. Find the volume of the solid generated by revolving about the $y$-axis the region bounded by $y^{2}=4 x$, the $y$-axis, and the line $y=2$.
5. Find the volume of the solid generated by revolving about the $x$-axis the region bounded by $y=\sqrt{x}$, and $y=x^{2}$.
