

Determine the derivatives of the following unless the directions in the problem ask for something else. You may do your work on a separate sheet of paper.

1) Prove $\frac{d}{dx}[\cot x] = -\csc^2 x \cdot dx$

2) Prove $\frac{d}{dx}[\csc x] = -\csc x \cot x \cdot dx$

3) $\frac{d^{80}}{dx^{80}}[\cos 2x] =$

4) Prove $\frac{d}{dx}[\sec x] = \sec x \tan x \cdot dx$

5) $\frac{d^2}{dx^2}[\sin^2 x + \cos^2 x] =$

6) Find y' if $y = \cos^2(4x)$

7) $\frac{d}{dx}\left[\frac{1}{\sin^2 x}\right]$

8) If $f(x) = 2 \sin x$, then find $\frac{d}{dx}(f'(x))$.

9) $\frac{d}{dx}[\sin x^2]$

10) $y = \sqrt{x \sin x}$

11) $\frac{d^2}{dx^2}(\sec x)$

12) $\frac{dy}{dx}[\sin^2(x^2 + 2)]$

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13) If $h(x) = f(g(x))$, find $h'(4)$ if $g(4) = -2$, $g'(4) = -4$, and $f'(-2) = 2$.

14) If $y = t^2$ and $x = 7t + 4$, find $\frac{dy}{dx}$.

15) If $y = 2u^2$ and $u = 4x - 7$, find $\frac{dy}{dx}$.