Example A4: The function $f$ is defined and differentiable on the interval $[-6,8]$ and satisfies $f(0)=-3$. The graph of $y=f^{\prime}(x)$, the derivative of $f$, consists of a semicircle and six line segments as shown in the figure below.
a) Find $f(6)$ and $f(-6)$. (2)
b) Find the $x$ coordinate of each point of inflection of the graph of $y=f(x)$ on
 $-6<x<8$. Explain your reasoning. (1)
c) Find the equation of the tangent line to $f$ at $x=-6$. Use this line to approximate $f(-5.9)$. Is this value an over-approximation or under-approximation? Explain. (2)
d) Find the absolute maximum value of $f(x)$ on $-6 \leq x \leq 8$. Justify your answer. (2)
e) The function $g$ is defined as $g(x)=\frac{x^{2}}{2}-f(x)$. Find the values of $x$ for each critical point of $g$ on $-6<x<8$. Explain your reasoning. (2)

