

Practice

Infinite Sequence and Series

Find each limit, or state that the limit does not exist and explain your reasoning.

1. $\lim_{n \rightarrow \infty} \frac{n^2 - 1}{n^2 + 1}$

2. $\lim_{n \rightarrow \infty} \frac{4n^2 - 5n}{3n^2 + 4}$

3. $\lim_{n \rightarrow \infty} \frac{5n^2 + 1}{6n}$

4. $\lim_{n \rightarrow \infty} \frac{(n - 1)(3n + 1)}{5n^2}$

5. $\lim_{n \rightarrow \infty} \frac{3n - (-1)^n}{4n^2}$

6. $\lim_{n \rightarrow \infty} \frac{n^3 + 1}{n^2}$

Write each repeating decimal as a fraction.

7. $0.\overline{75}$

8. $0.\overline{592}$

Find the sum of each infinite series, or state that the sum does not exist and explain your reasoning.

9. $\frac{2}{5} + \frac{6}{25} + \frac{18}{125} + \dots$

10. $\frac{3}{4} + \frac{15}{8} + \frac{75}{16} + \dots$

11. **Physics** A tennis ball is dropped from a height of 55 feet and bounces $\frac{3}{5}$ of the distance after each fall.

- Find the first seven terms of the infinite series representing the vertical distances traveled by the ball.
- What is the total vertical distance the ball travels before coming to rest?