

**KNOW THE FOLLOWING THREE THEOREMS:**

<p>A. <math>\lim_{x \rightarrow 0} \frac{\sin \square}{\square} = 1</math></p>	<p>B. <math>\lim_{x \rightarrow 0} \frac{\square}{\sin \square} = 1</math></p>	<p>C. <math>\lim_{x \rightarrow 0} \frac{1 - \cos \square}{\square} = 0</math></p>
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**Examples:**

<p>1. <math>\lim_{x \rightarrow 0} \frac{\sin 3x}{x} \Rightarrow \lim_{x \rightarrow 0} \frac{\sin 3x}{x} \cdot \left[ \frac{3}{3} \right] \Rightarrow \lim_{x \rightarrow 0} 3 \left[ \frac{\sin 3x}{3x} \right] = \boxed{3}</math></p>	<p>2. <math>\lim_{x \rightarrow 0} \frac{1 - \cos 7x}{x} \Rightarrow \lim_{x \rightarrow 0} \frac{1 - \cos 7x}{x} \cdot \left[ \frac{7}{7} \right] \Rightarrow \lim_{x \rightarrow 0} 7 \left[ \frac{1 - \cos 7x}{7x} \right] = \boxed{0}</math></p>
<p>3. <math>\lim_{x \rightarrow 0} \frac{\tan 2x}{x} \Rightarrow \lim_{x \rightarrow 0} \frac{\cos 2x}{x} \Rightarrow \lim_{x \rightarrow 0} \frac{\sin 2x}{x \cos 2x} \Rightarrow \lim_{x \rightarrow 0} \frac{\sin 2x}{x} \cdot \left[ \frac{2}{2} \right] \Rightarrow \lim_{x \rightarrow 0} \frac{2}{2x} \left[ \frac{\sin 2x}{2x} \right] \Rightarrow \lim_{x \rightarrow 0} \frac{2}{x} \Rightarrow \lim_{x \rightarrow 0} \frac{2}{\cos 2x} = \boxed{2}</math></p>	

**Problems:**

<p>1. <math>\lim_{x \rightarrow 0} \frac{\sin \frac{1}{2}x}{x}</math></p>	<p>2. <math>\lim_{x \rightarrow 0} x \csc x</math></p>	<p>3. <math>\lim_{x \rightarrow 0} \frac{\sin 2x}{\sin x}</math></p>	<p>4. <math>\lim_{x \rightarrow 0} \frac{\sin ax}{x}, a \neq 0</math></p>
<p>5. <math>\lim_{x \rightarrow 0} \frac{\tan x}{x}</math></p>	<p>6. <math>\lim_{x \rightarrow 0} \frac{\sin 3x}{\sin 2x}</math></p>	<p>7. <math>\lim_{x \rightarrow 0} \frac{\sin 3x}{x}</math></p>	<p>8. <math>\lim_{x \rightarrow 0} \frac{\sin x}{2x}</math></p>
<p>9. <math>\lim_{x \rightarrow 0} \frac{3 \sin x}{x}</math></p>	<p>10. <math>\lim_{x \rightarrow 0} \frac{\sin 3x}{5x}</math></p>	<p>11. <math>\lim_{x \rightarrow 0} \frac{\sin 4x}{2x}</math></p>	<p>12. <math>\lim_{x \rightarrow 0} \frac{3x}{\sin x}</math></p>
<p>13. <math>\lim_{x \rightarrow 0} \frac{\sin^2 x}{x}</math></p>	<p>14. <math>\lim_{x \rightarrow 0} \frac{\sin ax}{\sin bx}</math></p>	<p>15. <math>\lim_{x \rightarrow 0} \frac{\sin^4 2x}{4x^4}</math></p>	<p>16. <math>\lim_{x \rightarrow 0} \frac{\sin 5x}{5x}</math></p>
<p>17. <math>\lim_{x \rightarrow 0} \frac{1 - \cos(2x)}{2x}</math></p>	<p>18. <math>\lim_{x \rightarrow 0} \frac{x+2}{\cos x}</math></p>	<p>19. <math>\lim_{x \rightarrow \frac{\pi}{4}} (\tan x)</math></p>	<p>20. <math>\lim_{x \rightarrow 0} \frac{1 - \cos x}{\sin^2 x}</math></p>