

Unverified Key for 1<sup>st</sup> Semester Review Limits, Continuity, Derivatives, PVA, F, F', F'', and Related Rates (I will review these answers when I can and do the few missing too). If you think any are in error, please let Mike know. I did them pretty fast.

Thanks

1.  $4x + 3$
2. 0
3.  $-3/4$
- 4a. -1
- 4b. 2
- 4c.  $3/2$
- 4d. 2
- 4e. 1
- 4f. DNE
5. DNE
6.  $F(2) = \text{DNE}$   $\lim_{x \rightarrow 2} f(x)$  as  $x$  approaches 2 is 6
7.  $2/3$
8. -2
9. 27
10. 1
11. 0
12. 2
13. hole at  $x = -3$  and asymptote at  $x = -2$
14. Discontinuity at  $x = 1$ , jump discontinuity
15.  $b = 2$  and  $a = 1$
- 16a. c, d
- 16b. c, d, e, f, g
17.  $(x^3 - x^2 - 1)(2x) + (3x^2 - 2x)(x^2 + 2)$
18.  $(3x^2 + 30x - 12)/(x + 5)^2$
19.  $(2x^3 + 5x^2)^3 (6x^2 + 15x)$
20.  $(3x^5)/\sqrt{(x^2 - 9)} + 12x^3(x^2 - 9)$
21.  $-2\sin(x)\sin(2x) + \cos(x)\cos(2x)$
22.  $6(\tan^2 2x)(\sec^2 2x)$
23.  $-2\cot(2x)/\sin(2x)$
24.  $e^{x^2}(2x)$
25.  $-e^{-x}(\cos(e^{-x}))$
26.  $2/x$
27.  $\text{Cot}(x)$

28a. b    28b. d

29.  $y-5 = -1(x+1)$                       30.  $Y+3 = -3(x-1)$                       31. 2.5

32a.  $y-(3/2)(\sqrt{3}) = 3(x-\pi/6)$                       32b. 2.527

32c.  $y = \text{TBD}$                       32d.  $\theta = .6234$

33a.  $x = -2$  rel min                      33b. inc  $(-2, \infty)$ ; dec  $(-\infty, -2)$

34a. 2.2/.75                      34b. 4                      35a. .33                      35b. .4

36.  $f'(3) < f(3) < f''(3)$                       37. TBD

38a. to the right, 8 ft/sec    38b. 0

38c. Speeding up (0,6) and (10, 16)                      38d.  $(2/5)$  ft/sec<sup>2</sup>

38e. 3 times

39a.  $v(t) = 3x^2 - 18x + 23$                       39b. moving to the left (0, 4.155)

39c. to the left and position is 3    39d.  $a(t) = 6x - 18$

39e.  $x(4) = -3$ ft     $v(4) = -1$  ft/sec, moving to the left 1 ft/sec  $a(t) = 6$  ft/sec<sup>2</sup>

40. average velocity -2 ft/sec    b. at  $t=2$  IROC equals AROC

41a. 488 ft                      41b. (4, 12)                      41c.  $v(t) = 3t^2 - 2$

41d. 190 ft/sec                      41e.  $\sqrt{6/3} < t < 12$                       41f. 95 ft/sec

41g.  $t = \sqrt{97/3}$                       41h.  $a(t) = 6t$                       41i. 48 ft/sec<sup>2</sup>

41j. TBD

42a. -1.819    42b.  $(0, \pi)$                       42c.  $-\cos(t)$ cm/s    42d. .832 cm/s

42e.  $(\pi/2, 3\pi/2)$                       42f.  $-.136$  cm/s<sup>2</sup>    42g. 1.638 and 4.780 seconds

42h.  $2\sin(t)$  cm/s<sup>2</sup>    42i. 1.819cm/s<sup>2</sup>    42j. TBD

43. Absolute extrema at  $x = -2$  max and  $x = 2$  min

44. Local extrema at  $x=-1/3$  and  $2$  since  $f'$  goes from pos to neg or vice versa

45.  $f''(a) < f'(a) < f(a)$  conc down, 0, positive slope

46.  $x=-1/2$  point of inflection since  $f''$  goes from + to - there

47.  $x=0$  and  $x=4$  are points of inflection since  $f''$  changes sign there

48.  $f$  increasing on  $(-\infty, 0)$

49.  $f$  concave down where  $f'' < 0$  all  $x$   $f$  is concave down

50.  $x = -2, 4/3$  local extrema

51. same as 50

52a.  $f(x) = -x+6$  (2,4) and  $f(x) = x+2$  (4,6)

52b.  $f$  has an abs max at  $x=2$

52c. T            52d. F

53a.  $x=-4, 0, 4$  since  $f' = 0$  or DNE there

53b.  $(-6, -4)$  and  $(0, 4)$  inc    $(-4, 0)$  and  $(4, 6)$  dec since  $f'$  pos inc and  $f'$  neg dec

53c. Points of inflection:  $x=-2$  and  $2$  since  $f''$  pos to neg there

53d. conc up  $(-6, -4)$  and  $(-4, -2)$  and  $(2, 4)$  and  $(4, 6)$  since  $f''$  pos there

Conc down  $(-2, 0)$  and  $(0, 2)$  since  $f''$  neg there

54.  $y' = -6x$             55.  $(-y-3x^2 y^2)/(2x^3 y+x)$

56.  $y'' = (y'y' - 3)/(1+y')$

57a.  $(4xy-8)/(6y^2-2x^2-1)$             57b.  $xy=2$

58a.  $(16x-5y)/(5x+3y^2)$             58b.  $y+1=3(x-4)$             58c.  $K=-.4$

59 a.  $9/5$  ft/sec            59b.  $24/5$  ft/sec

60a.  $-2/\sqrt{3}$  ft/sec            60b.  $-80/\sqrt{3}$  rad/sec

61.  $-.0404 \text{ ft/sec}$